Abstract. There is a variety of different cosmogenic radionuclide-based reconstructions of solar activity variations for the past. Especially the longer-term changes and the absolute levels of past solar activity are uncertain as it is illustrated by the differences between these reconstructions. On the one hand there are differences between \(^{10}\text{Be}\) and \(^{14}\text{C}\) records that are commonly used as proxies for the varying solar modulation of galactic cosmic rays. On the other hand estimates of past changes in the geomagnetic shielding also include relatively large uncertainties. Here, we concentrate on variations in cosmogenic radionuclide records on time scales of 50 to 500 yr. We show that these are to a large extent independent of the geomagnetic field intensity. The range of variability of cosmogenic radionuclide records allows us to set constraints about long-term changes in solar activity. These records indicate that present solar activity levels were reached or exceeded regularly in the past.

1 Introduction

Cosmogenic radionuclides are the most reliable indirect recorders of past changes in solar activity. These particles are produced in the cascade of reactions in the atmosphere initiated by high-energy galactic cosmic rays (GCRs) (e.g. Lal and Peters, 1967). The solar and geomagnetic shielding of cosmic rays and consequently the production rates of cosmogenic radionuclides can be exploited for solar activity and geomagnetic field reconstructions. However, variations in the transport and deposition of cosmogenic radionuclides from their origin into the natural archives can complicate such calculations. For example, \(^{10}\text{Be}\) has an average atmospheric residence time in the order of a year during which it is generally well mixed in the atmosphere. However, if the atmospheric circulation or deposition pattern were to change significantly during a longer period, \(^{10}\text{Be}\) records would partly reflect the transport or deposition change in the atmosphere and not only the production signal. In the following we will also consider radiocarbon (\(^{14}\text{C}\)). After the production \(^{14}\text{C}\) oxidises to \(^{14}\text{CO}_2\) and gets incorporated into the carbon cycle. Therefore, \(^{14}\text{C}\) records also reflect carbon cycle-related processes.

There are several reconstructions of past changes in solar activity for the Holocene period (e.g. Knudsen et al., 2009; Solanki et al., 2004; Vonmoos et al., 2006; Steinilber et al., 2008). All of them are based on cosmogenic radionuclides but, while different radionuclide records agree generally well with respect to their short-term changes, there are differences in the long-term changes of \(^{10}\text{Be}\) and \(^{14}\text{C}\) records on time scales of millennia (Muscheler et al., 2004; Vonmoos et al., 2006). The origins of the differences are not yet resolved but they lead to a significant divergence in the reconstructed solar activity levels based on \(^{10}\text{Be}\) and \(^{14}\text{C}\) (Vonmoos et al., 2006).

In addition to differences between \(^{10}\text{Be}\) and \(^{14}\text{C}\) records there is also considerable uncertainty in the reconstructed geomagnetic field intensities (e.g. Knudsen et al., 2008). Nevertheless, reliable reconstructions of past changes in geomagnetic field intensity have been a prerequisite for an accurate separation between geomagnetic and solar influences on the \(^{10}\text{Be}\) and \(^{14}\text{C}\) production rates.

In the following we will present a method to constrain past changes in solar variability that is largely independent of the geomagnetic field uncertainties and that is not influenced by the long-term differences between the radionuclide records. Therefore, in contrast to earlier calculations our conclusions are not affected by these two major uncertainties for solar activity reconstructions. We will begin with a short review of the latest results on the local interstellar galactic cosmic ray spectra since these determine the possible range of variability.
that can be expected from solar activity variations. This will be followed by a discussion of the geochemical behaviour of $^{14}$C and $^{10}$Be and potential biases in the reconstructed variations in $^{14}$C and $^{10}$Be production rates. We will discuss the robustness of our results via comparison of the $^{10}$Be and $^{14}$C-based solar activity estimates.

2 Theoretical background

2.1 Cosmogenic radionuclide production

Cosmogenic radionuclides are produced by high-energy cosmic rays that manage to enter the Earth’s atmosphere through a shielding due to the heliospheric- and geo-magnetic field. $^{10}$Be is produced in spallation reactions while $^{14}$C is mainly produced by thermal neutrons captured by nitrogen (Lal and Peters, 1967). The production processes are well understood and can be modelled quantitatively (e.g. Masarik and Beer, 1999, 2009). These calculations require the knowledge of the primary GCR spectrum reaching Earth. For the interpretation of cosmogenic radionuclides the force-field approximation is a practical simplification (Gleeson and Axford, 1968). It describes the solar-modulated GCR spectra with a single parameter, the so-called solar modulation function $\Phi$. With higher solar activity (and larger $\Phi$) the lower energy particles get preferentially deflected and, in the vicinity of Earth, the GCR spectrum is depleted in low energy particles. Important for our considerations is also the GCR spectrum outside the heliosphere the so-called local interstellar spectrum (LIS). It determines the increase in GCRs from e.g. todays values compared to a period of low or absent solar magnetic shielding.

Figure 1 shows a variety of published GCR proton spectra outside the heliosphere i.e. with absent solar shielding. The different publications disagree significantly especially in the lower energy part of the LIS. This is mainly due to the fact that the relatively strong solar modulation since the beginning of such measurements obscured the lower energy range of the LIS. However, as the Voyager satellites approach the modulation boundary, the heliopause, it is possible to gain new insights into the GCR spectra. Using these data Webber and Higbie (2009, 2010) suggested updated GCR spectra (blue line in Fig. 1). Compared to earlier estimates (as e.g. Burger et al., 2000; Garcia-Munoz et al., 1975) there are fewer lower energy protons. This has profound effects on the interpretation of cosmogenic radionuclide records. Fewer particles in the local interstellar spectrum mean that the difference to the present GCR spectrum at Earth is smaller. Consequently, the newer LIS estimates imply a reduced increase in cosmic rays (and consequently in cosmogenic radionuclide production rates) that can be expected with lower or absent solar shielding (Webber and Higbie, 2010). In the following we will use the results of Masarik and Beer (1999, 2009) for our quantitative considerations. They based their calculations on the LIS published by Garcia-Munoz et al. (1975).

As a first approximation the results by Masarik and Beer (1999, 2009) can be transferred to other LIS models by adjusting the modulation function to the respective LIS spectra. Usoskin et al. (2005) suggested such conversion relationships optimized for GCR spectrum at 1 AU. Concentrating on the energy range relevant for the $^{10}$Be production Steinihilber et al. (2008) found similar relationships. For example, a cosmic ray spectrum at Earth that corresponds to a modern solar 11-yr cycle minimum can be described with a solar modulation function of 400 MeV in connection to the Burger et al. (2000) spectrum. Since the LIS by Garcia-Munoz et al. (1975) has fewer protons at lower energies a correspondingly smaller solar modulation function would represent a similar spectrum with this LIS. The energy dependence is different for the different spectra and, therefore, the suggested linear conversions of the solar modulation functions are just a first order approximation. Instead of simply comparing the spectra with the different LIS and different solar modulation functions it is more accurate to weigh the spectra with the yield functions for the radionuclide production rates (e.g. Webber and Higbie, 2003). For example, with the new LIS suggested by Webber and Higbie (2010) we get the same $^{10}$Be production rate as with the LIS from Garcia-Munoz et al. (1975) modulated with a solar modulation function of about 160 MeV.

In conclusion, there are uncertainties in the different LIS suggestions and we have chosen to use the results based on the LIS published by Garcia-Munoz et al. (1975). Recent LIS suggestions are more deficient in low energy cosmic rays which leads to a more restricted range for cosmogenic radionuclide production rate variations. New results on the LIS could lead to minor modifications for our analysis but there are methods how, for example, the results of Masarik and

![Figure 1: Published GCR spectra for protons. There are significant differences in the lower energy range of the spectra and the most recent estimates (Webber and Higbie, 2010) suggest a smaller number of lower-energy protons in the spectra.](image-url)
Beer (1999, 2009) can be transferred to other LIS models.

### 2.2 $^{10}$Be and $^{14}$C production rate variability

Masarik and Beer (1999, 2009) calculated the $^{10}$Be and $^{14}$C production rates in the atmosphere for a suite of solar and geomagnetic shielding scenarios. From their results we can obtain estimates of how much the globally averaged production rates can change depending on solar and geomagnetic shielding. Especially important for the following discussion is the increase in $^{10}$Be and $^{14}$C production rates that we can expect if the solar modulation would be absent, i.e. if GCRs can enter the solar system without being partly deflected by the Sun.

The relative increase of the $^{10}$Be and $^{14}$C production rates with lower solar shielding remained virtually unchanged with the new updated calculations of Masarik and Beer (2009). The results suggest that the globally averaged $^{10}$Be production rate increases by 52% for absent solar shielding relative to an average $^{10}$Be production rate during the last 60 yr ($\Phi \approx 700$ MeV). The $^{14}$C production rate reacts more sensitively to variations in solar shielding. The globally averaged $^{14}$C production rate is estimated to increase by about 70% from a recent average solar activity to absent solar shielding (Masarik and Beer, 1999, 2009). Considering the recent revisions to the LIS these two numbers are rather upper estimates since, as mentioned before, the potential GCR increase compared to today is likely to be smaller as suggested by the LIS used by Masarik and Beer (1999, 2009).

Even though the $^{10}$Be and $^{14}$C production rates depend on the interplay between geo- and solar magnetic shielding the relative increases in $^{10}$Be and $^{14}$C production rates are surprisingly independent of the geomagnetic field intensity. Figure 2 shows the globally averaged $^{14}$C production rates as a function of the solar modulation (Masarik and Beer, 1999). The different lines show this relationship for different geomagnetic field intensities. In fact almost all the curves lie on top of each other and indicate the same relative increase in the globally averaged $^{14}$C production rate of about 70% for a change of the solar modulation function from 700 MeV to 0 MeV. Only for very low geomagnetic field intensities ($B=0$ and $B=1/4$ of today's values) these results suggest a larger increase.

### 2.3 Geochemical behaviour of $^{10}$Be and $^{14}$C

After the production $^{10}$Be and $^{14}$C have a very different geochemical behaviour. $^{14}$C oxidises to CO$_2$ and enters the carbon cycle (e.g. Siegenthaler et al., 1980). By contrast, $^{10}$Be gets attached to aerosols and becomes deposited onto the Earth's surface within 1 – 2 yr (e.g. McHargue and Damon, 1991). Therefore, changes in these processes, such as a climate change, also affect the radionuclide concentrations in a different way. Hence, the different geochemical behaviour can be used to extract and isolate the common production rate signal in $^{10}$Be and $^{14}$C records, and it allows us to study climate-related influences on $^{10}$Be and $^{14}$C.

Since $^{14}$C enters the carbon cycle its concentration in the atmosphere depends not only on the $^{14}$C production rate but also on the exchange processes between atmosphere, biosphere, mixed layer and deep ocean. Freshly produced $^{14}$C, therefore, adds to a large reservoir of previously produced $^{14}$C. Hence, solar-induced $^{14}$C variations appear only damped and delayed in the atmospheric $^{14}$C concentration. A carbon cycle model is required to take these processes into account in order to reconstruct the production signal. Delaygue and Bard (2010) show the attenuation and phase lag of atmospheric $^{14}$C concentrations with respect to the $^{14}$C production rate for a variety of different carbon cycle models. For typical solar changes on time scales of e.g. 200 yr they obtain an attenuation factor of about 0.05 to 0.06 and a phase lag of about a tenth of the cycle length. This means that a solar cycle with a duration of 200 yr and a $^{14}$C production rate variation of e.g. 20% will produce an atmospheric $^{14}$C variation of about 1% with maxima and minima that are delayed by about 20 yr. In the following we will show results from a box-diffusion carbon cycle model (Oeschger et al., 1975; Siegenthaler, 1983). The model-based attenuation factors and phase lags are in the same range as mentioned by Delaygue and Bard (2010) and results from the box-diffusion model agree well with results from more advanced 3-D carbon cycle models (Muscheler et al., 2007).

$^{14}$C has the advantage that the atmospheric residence time is long enough to allow $^{14}$C to become well mixed in the
atmosphere. This means that latitudinal differences in the 
$^{14}$C production rates should not be visible and that the atmo-
spheric $^{14}$C concentrations measured at any latitude, indeed
reflect the globally averaged $^{14}$C production rates. Changes
in the carbon cycle can potentially have an impact on the $^{14}$C
concentration in the atmosphere. However, atmospheric $^{14}$C
concentrations are not very sensitive to carbon cycle changes
(e.g. Siegenthaler et al., 1980) and, therefore, such influences
should be minor during the climatically stable Holocene pe-
tiod that we discuss in this paper.

By contrast to $^{14}$C, $^{10}$Be stays in the atmosphere and is
transported and deposited following the atmospheric aerosols
within circa 1 yr only. Due to the geomagnetic shielding the
solar induced changes in the radionuclide production rates
are larger at the poles than at the equator. This has led to
suggestions that there could be a polar bias in $^{10}$Be records
from ice cores from the polar ice caps (Bard et al., 1997;
Mazaud and Bender, 1994). This has recently been investi-
gated in detail by employing three-dimensional general cir-
culation models that also include aerosol chemistry (Field et
al., 2006; Heikkilä et al., 2008, 2009). These studies show
that $^{10}$Be, especially the most modulated fraction at high lat-
itudes, is mainly produced in the stratosphere. The strato-
sphere is stably layered allowing for a long residence time of
aerosols and a smoothing out of gradients in aerosol concen-
trations. Thereafter, $^{10}$Be is transported into the troposphere,
mainly at mid-latitudes, where it is subjected to tropospheric
transport and removal by rain or dry deposition.

The atmosphere is a non-linear system and the models re-
quire high resolution in order to fully resolve the transport pro-
cesses of atmospheric particles. In any numerical model
there is always some numerical diffusion in addition to physi-
cal diffusion. Numerical diffusion arises when, for modelling
purposes, continuous systems are discretized and exchange
processes are calculated in discrete spatial steps. The use of
a coarse resolution tends to increase numerical diffusion.
Unfortunately it is impossible to distinguish between nu-
merical and physical diffusion. If numerical diffusion over-
rules physical diffusion in the model particles spread out too
rapidly in horizontal and in vertical direction. This would
lead to a too short residence time of $^{10}$Be in the stratosphere
and $^{10}$Be would be transported too rapidly to lower levels.
If this occurs to particles at polar latitudes, they would not
undergo the transport over the mid-latitudes, and the change
in the modelled deposition fluxes at polar latitudes would be
larger than in reality. The different response of polar deposi-
tion to production changes between ModelE (showing a po-
ar bias; Field et al., 2006) and ECHAM5-HAM (no polar bias;
Heikkilä et al., 2008, 2009) can probably be explained by the
different resolution of the models. Intercomparison of
these models indicates that mixing of aerosols is limited in
ModelE as, compared with other models, it has the coarsest
resolutions (Textor et al., 2006).

The model study by Heikkilä et al. (2009) quantifies the
fractions of $^{10}$Be transported to polar latitudes from differ-
ent parts of the atmosphere. In present day climate and so-
lar activity ca. 65% of $^{10}$Be is produced in the stratosphere,
where it undergoes throughout mixing during its long resi-
dence time. A polar bias could be possible if 1) the fraction
of $^{10}$Be produced locally in the polar troposphere was large
or 2) $^{10}$Be produced in the polar stratosphere was deposited
rapidly after production before undergoing mixing. Accord-
ing to Heikkilä et al. (2009) the fraction of $^{10}$Be produced
in the polar troposphere is 10 − 20% of the polar deposition
fluxes. This fraction is not large enough to contribute to a
detectable polar bias because the production modulation is
quite weak in low latitudes. The strongly modulated $^{10}$Be
produced in the polar stratosphere would lead to a polar bias
if it was deposited directly to polar latitudes. The process re-
ponsible for such direct deposition is gravitational settling.
It is included in the models but contributes only to less than
5% of the total deposition. The lack of evidence for 1) or 2)
in the model study explains the absence of a polar bias.

The modelling shows that, if significant changes in the
precipitation or atmospheric circulation patterns have taken
place in the past, the relative changes of $^{10}$Be concentra-
tions could potentially have been influenced during the pe-
riod of change in regions where patterns shifted (Heikkilä
et al., acc.). However, it is not expected that these could
lead to systematic alterations of the amplitudes in the $^{10}$Be
records if there is no persistent connection between cosmic
ray/solar variations and climate/$^{10}$Be deposition in the region
where the $^{10}$Be record originates. Such potential biases are
best detected by comparison to other cosmogenic radionu-
clide records, as is made in this study.

In the following we will base our discussion on the most
recent high-resolution climate model results that suggest that
there is no systematic polar bias in the $^{10}$Be data. We will
evaluate this hypothesis by comparing $^{10}$Be and $^{14}$C records.

3 $^{14}$C-based solar variations during the last 1000 years

Figure 3 shows the $^{14}$C production rate reconstruction
(Muscheler et al., 2007) based on the Intcal04 $^{14}$C data
(Reimer et al., 2004) and an annual $^{14}$C record measured by
Stuiver and Braziunas (1998). There has been a debate on
how to best normalise this record since fossil fuel burning
(Suess, 1953) and nuclear bomb tests have significantly in-
fluenced the $^{14}$C levels in the atmosphere. While the fossil
fuel burning can be included in the calculation of the $^{14}$C pro-
duction rate (Muscheler et al., 2007) it, however, adds to the
uncertainties of the $^{14}$C trend in the first part of the 20th
century. The nuclear weapon tests completely overshadow the
natural $^{14}$C variations and make solar activity reconstructions
impossible for the period of the strong anthropogenic $^{14}$C in-
crease in the second part of the 20th century. Therefore, there
is only a limited overlap between $^{14}$C-based and instrumen-
tal cosmic ray records such as neutron monitor data and ion-
zation chamber data (McCracken and Beer, 2007). Conse-
sequently, the connection between the $^{14}$C record and modern cosmic ray observations includes some uncertainties. $^{10}$Be records, available up to date, cannot resolve these normalisation uncertainties since there are unexplained differences between records from Greenland and Antarctica (e.g. Raisbeck and Yiou, 2004). The uncertainties in relating today’s solar activity to the cosmogenic radionuclide-based solar activity reconstructions can be reduced by applying the amplitude considerations outlined above.

For example, we can assume that the maximum levels in cosmogenic radionuclide production rates during the Maunder minimum (from approx. 1645 to 1715 AD) correspond to a complete absence of solar shielding of galactic cosmic rays (upper dotted line in Fig. 3). This would correspond to the lowest possible limit of solar activity during the Maunder minimum. As mentioned above, Masarik and Beer (1999, 2009) estimated a 70% increase in the global $^{14}$C production rate from recent average solar activity levels to an absent solar shielding. Therefore, the lower dotted line in Fig. 3 indicates average solar activity levels of the last 60 yr if the Maunder minimum indeed was characterized by an intermittent complete lack of solar modulation of cosmic rays. It indicates even higher levels if solar modulation was not completely absent during the Maunder minimum.

Geomagnetic field changes during the last 1000 yr are of minor importance in this discussion as long as one does not compare periods that are characterised by strongly varying geomagnetic field strength. For example, with these considerations one can infer that solar activity levels before and after the Maunder minimum must have been similar or higher compared to average solar activity levels during the last 60 yr. However, it is problematic to compare Maunder minimum levels with e.g. the solar modulation around 1000 AD since there was a considerable long-term geomagnetic field decrease during the last 3000 yr (e.g. Knudsen et al., 2008). This has led to an increase in the $^{14}$C production rate during this period. For reliable solar activity reconstructions of the absolute solar modulation levels this has to be corrected for. The large uncertainties in the geomagnetic field reconstructions then transfer directly into uncertainties in the solar activity reconstructions.

We can remove this uncertainty using the results shown in Fig. 2. As long as we concentrate on relative changes on relatively short time scales, where we can assume that geomagnetic field changes were minor, we can infer robust lower limits of solar activity in the past. Geomagnetic field uncertainties do not influence the results as long as very low geomagnetic field intensities are not reached. This was the case for example during the last approx. 11 500 yr (The Holocene) when geomagnetic field intensities below half of the present levels were never reached (e.g. Knudsen et al., 2008).

To conclude, Fig. 3 suggests that solar modulation levels around 1400, 1600 and 1800 AD were similar or higher than the average solar activity levels during the last 60 yr since the relative increase in the $^{14}$C production rate is similar to the increase that we can expect from today’s solar shielding to an absent shielding. Geomagnetic field variations can be neglected in this discussion since we concentrate on changes on short time scales (e.g. we compare Maunder minimum levels (around 1700 AD) to the solar maxima just before and after the Maunder minimum) where the geomagnetic field intensity variations are insignificant for the $^{14}$C variability.

4 $^{10}$Be and $^{14}$C during the Holocene

The amplitude discussion exemplified for the last 1000 yr can be applied to the complete Holocene period. In this case it is even harder to accurately reconstruct solar activity levels since geomagnetic field uncertainties increase further back in time. In addition, cosmogenic radionuclide records exhibit unexplained differences on longer time scales (Vonmoos et al., 2006; Muscheler et al., 2004).

We will discuss the $^{10}$Be records from the two neighbouring Greenland Ice Core Project (GRIP) and Greenland Ice Sheet Project 2 (GISP2) ice cores from Central Greenland (Vonmoos et al., 2006; Muscheler et al., 2004; Finkel and Nishizumi, 1997). In addition, we will use the $^{14}$C production rate inferred from the $^{14}$C calibration record (Muscheler et al., 2005; Reimer et al., 2004). Reconstructing and discussing the $^{14}$C production rate removes as much as possible known effects of the carbon cycle on the atmospheric $^{14}$C concentration (such as e.g. the dampening effect). Comparison of the radionuclide data to geomagnetic field reconstructions have shown that it is difficult to distinguish between solar and geomagnetic field influences on the cosmogenic radionuclides. Often it is assumed that geomagnetic field changes have a significant influence on the radionuclide production rates on longer time scales whereas solar activ
ity changes act rather on shorter time scales. It is unclear if this distinction is justified and which time scales are best to divide up solar and geomagnetic field changes. It has been shown that on time scales of 3000 yr and longer the variations in cosmogenic radionuclides can be well explained by geomagnetic field changes (Muscheler et al., 2005; Wagner et al., 2000). Using high-resolution geomagnetic field reconstructions Snowball and Muscheler (2007) showed that the geomagnetic field influence becomes important on time scales of 500 yr and longer. However, these results depend on the limited resolution and accuracy of the geomagnetic field reconstructions.

In the following we will assume that on time scales shorter than 500 yr the solar influence on cosmogenic radionuclides is dominant and, due to limited temporal resolution of the data, we concentrate on time scales longer than 50 yr (100 yr respectively) to illustrate the solar activity changes on centennial time scales. Figure 4 shows the low-pass filtered (cut-off frequencies 1/50 yr and 1/100 yr, respectively) 10Be and 14C records divided by their longer-term changes on time scales of 500 yr and longer (division by the data after filtering with a cut-off frequencies of 1/500 yr). Thus, we infer the relative variations of the cosmogenic radionuclide after applying the following procedure:

\[
\text{Var}_{14C} = \frac{14 \text{C}_{lp50(lp100)}}{14 \text{C}_{lp500}} \quad (1)
\]

and

\[
\text{Var}_{10\text{Be}} = \frac{10 \text{Be}_{lp50(lp100)}}{10 \text{Be}_{lp500}} \quad (2)
\]

\(lp50, lp100\) and \(lp500\) denote the different applied low-pass filters. This means that we focus exclusively on the relative variations around the longer-term mean. Consequently, we remove long-term changes in solar activity on time scales longer than 500 yr but we also remove, as much as possible, the geomagnetic field uncertainty in the discussion. Again, by assuming that the maximum radionuclide production rates correspond to absent solar shielding (as a lower limit) we can obtain lower limits for solar activity levels throughout the Holocene.

Even with the absent 11-yr cycle and any additional solar variations on time scales shorter than 50 yr we observe that the 14C variations are often close to the 70% range from an absent solar modulation to average solar modulation levels of the last 60 yr. This implies that e.g. around 5500 yr BP solar activity levels had to exceed the levels that we observed during the satellite era. It is also clear that there are periods of a generally more stable solar activity where the range of variability is smaller (e.g. around 3500 yr BP). Due to uncertainties in the 10Be and 14C data and the geomagnetic field reconstructions any conclusion about absolute solar activity levels are uncertain. Periods of decreased variability could represent generally increased or decreased solar modulation or a mix thereof. During periods of less expressed solar variations on centennial time scales we see stronger activity in the shorter-term range (e.g. 88 yr cycle – see thin lines in Fig. 4).

The 10Be and 14C variations agree generally very well. However, the 10Be data suggests an even larger range of variability in solar modulation as the 14C data considering the stronger sensitivity of 14C production rate variations compared to 10Be. If we look at the suggested 52% range from absent solar shielding to recent solar activity levels we ob-

![Fig. 4. Relative variations in the 10Be concentrations from the GRIP (panel A: black) and GISP2 (panel A: blue) ice cores from Central Greenland and the 14C production rate (panel B). The grey shading indicates the range of variability from absent solar modulation to average solar activity during recent solar cycles. The thick lines show variations on time scales between 100 and 500 yr and the thin lines between 50 and 500 yr (details: see text).](image-url)

**Table 1.** Standard deviations of normalised production rate variations from Fig. 4 for the different radionuclide records and different periods of overlap. For 10Be the numbers in brackets indicate the corresponding values for the 10Be flux (Flux = 10Be concentration*accumulation rate*density of ice) which takes into account the potential influence of a varying snow accumulation rate on the 10Be deposition rate. For 14C the numbers in brackets indicate the variations diminished by about 25% to account for the expected production rate differences between 10Be and 14C.

<table>
<thead>
<tr>
<th>Period Data set</th>
<th>11 600 – 9 400 yr BP</th>
<th>3 310 – 7 970 yr BP</th>
<th>310 – 9 400 yr BP</th>
</tr>
</thead>
<tbody>
<tr>
<td>14C production rate</td>
<td>0.101 (0.076)</td>
<td>0.099 (0.074)</td>
<td>0.098 (0.074)</td>
</tr>
<tr>
<td>(1/50 + 1/500 yr)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>14C production rate</td>
<td>0.093 (0.070)</td>
<td>0.084 (0.063)</td>
<td>0.087 (0.065)</td>
</tr>
<tr>
<td>(1/100 + 1/500 yr)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>GISP2 10Be</td>
<td>0.072 (0.085)</td>
<td>0.077 (0.093)</td>
<td>–</td>
</tr>
<tr>
<td>(1/50 + 1/500 yr)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>GISP2 10Be</td>
<td>0.070 (0.080)</td>
<td>0.071 (0.078)</td>
<td>–</td>
</tr>
<tr>
<td>(1/100 + 1/500 yr)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>GRIP 10Be</td>
<td>–</td>
<td>0.108 (0.113)</td>
<td>0.108 (0.111)</td>
</tr>
<tr>
<td>(1/50 + 1/500 yr)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>GRIP 10Be</td>
<td>–</td>
<td>0.082 (0.081)</td>
<td>0.085 (0.083)</td>
</tr>
<tr>
<td>(1/100 + 1/500 yr)</td>
<td></td>
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</tr>
</tbody>
</table>
serve that the $^{10}$Be data covers this range without longer interruptions during basically the complete Holocene period. This suggests that, based on the $^{10}$Be data, there is hardly any possibility for sustained solar activity levels below present day conditions. The difference in variability in the $^{10}$Be and $^{14}$C data is also illustrated by the comparison presented in Table 1. It shows the results of a simple calculation of the standard deviations around the mean of the data presented in Fig. 4. It indicates that the GISP2 and GRIP data have a significantly different range of variability and the variability of the GISP2 data lies very close to the range of variability in $^{14}$C (after accounting for the production rate differences). Calculating the $^{10}$Be flux does not change the overall picture but it increases the variability in the data slightly. The biggest difference, however, is apparent when we compare the $^{14}$C production rate and the GRIP $^{10}$Be data. The variability in the GRIP $^{10}$Be record is about 30% larger than the variability in the $^{14}$C data. Thus, the discussion of reasons behind the $^{10}$Be and $^{14}$C differences is important since the GRIP $^{10}$Be data sets stronger limits to past solar activity levels than the $^{14}$C data or the GISP2 $^{10}$Be data.

The GRIP and the GISP2 $^{10}$Be data have been measured in ice cores from Central Greenland that were recovered only 30 km apart from each other. Therefore, we do not expect systematic differences in the $^{10}$Be deposition rates at the two sites. The most obvious difference and likely reason behind the differences is the different temporal resolution of the records. The GRIP $^{10}$Be record has an average resolution of 5 yr and the GISP2 record has only an average resolution of 35 yr. This can explain about 10% of the difference between the GRIP and GISP2 data on time scales from 50 to 500 yr. We obtain this estimate from a calculation where we artificially reduced the resolution of the GRIP data by averaging these data onto the GISP2 time scale. The increased variability in the $^{10}$Be flux compared to the $^{10}$Be concentration also points to a time resolution issue. To calculate the flux we multiplied the $^{10}$Be concentration with the reconstructed snow accumulation rate. For this we retained the higher resolution accumulation rate record which then leads to the higher range of variability in the GISP2 (and GRIP) $^{10}$Be flux data. On the other hand, smoothing due to low data resolution can also minimize the influence of “weather noise” in the data. For example, the GRIP $^{10}$Be record includes high-resolution changes that cannot be interpreted in terms of production rate changes. These are removed to a large degree by concentrating on variations on time scales longer than 50 yr but they might still leave some imprint in the filtered records. In conclusion, it is very likely that the low-resolution GISP2 $^{10}$Be record underestimates the production rate variability. The variability in the high-resolution GRIP $^{10}$Be record represents short-term changes more accurately but it might also reflect processes unrelated to production rate changes.

Figure 4 suggests that all of the major peaks in the $^{10}$Be and $^{14}$C records are indeed related to production rate vari-

5 Discussion

The discussion of the relative amplitudes in cosmogenic radionuclide records allows us to infer lower limits for solar activity levels in the past. This approach is more robust than the traditional approach where geomagnetic field reconstructions with relatively large uncertainties were included in the calculation to isolate the solar signal. However, our approach still contains considerable uncertainties. In the following we will discuss these uncertainties and evaluate if they are likely to question the conclusions of our analysis.

Production rate uncertainties: We were basing our discussion on the results by Masarik and Beer (1999, 2009). Their updated calculations about the relative changes in the radionuclide production rates confirm earlier results and are also in agreement with the result by e.g. Lal (1988). It is important to note that this does not apply to the absolute levels of the radionuclide production rates that, however, do not play a role in our discussion. Using the updated local interstellar spectra Webber and Higbie (2010) inferred a more limited potential for solar induced variations on the $^{10}$Be production rate. They estimate a maximum possible increase of 1.5 for absent solar shielding compared to recent solar activity levels. Since this estimate refers to polar areas the globally averaged increase in the $^{10}$Be production rate is even smaller. This agrees with the discussion outlined above that fewer particles in the LIS reduce the potential for $^{10}$Be and $^{14}$C production rate increases. Therefore, we included relatively conservative estimates for $^{10}$Be and $^{14}$C production
rate increases. If we adopted the smaller values by Webber and Higbie (2010) we would obtain even stronger constraints about solar activity levels in the past i.e. an even reduced possibility for sustained periods of low solar activity levels.

Table 1 indicates that there are differences in the variability of the different radionuclide records. Interesting in this context is the suggested polar bias of the $^{10}\text{Be}$ data. The GRIP $^{10}\text{Be}$ data exhibits indeed a larger variability than the $^{14}\text{C}$ production rate data after it is corrected for the expected production rate differences. However, the figure is not consistent because the GISP2 $^{10}\text{Be}$ record does not show a larger variability than $^{14}\text{C}$. As discussed in Sect. 2.3., new model calculations show no realistic $^{10}\text{Be}$ pathways that could transfer an enhanced polar production rate signal into the troposphere (Heikkilä et al., 2008, 2009). Therefore, we regard a polar bias in the $^{10}\text{Be}$ data as an unlikely explanation for the main differences between GRIP $^{10}\text{Be}$ and $^{14}\text{C}$.

While $^{14}\text{C}$ is well mixed in the atmosphere on a global scale there are some uncertainties involved in the reconstruction of the $^{14}\text{C}$ production rate. It is unlikely that carbon cycle changes had a significant impact on the short-term changes in $^{14}\text{C}$ (Siegenthaler et al., 1980) but there are some uncertainties involved in the carbon cycle models itself. Delaygue and Bard (2010) show a range of model results that exhibit differences in the attenuation and phase lags of atmospheric $^{14}\text{C}$ changes. These uncertainties directly transfer into uncertainties in the reconstructed $^{14}\text{C}$ production rate. For example, for typical solar variations with durations of 200 yr Delaygue and Bards models have attenuation factors ranging from 0.05 to 0.06. This means that the reconstructed $^{14}\text{C}$ production rate can include biases in this range depending on the applied carbon cycle model. Our box-diffusion model (Oeschger et al., 1975; Siegenthaler, 1983) is at the lower limit in this attenuation range which implies that the reconstructed $^{14}\text{C}$ production rate is at the upper range of the models investigated by Delaygue and Bard (2010). Nevertheless, as mentioned above our model results agree well with newer 3-D carbon cycle models which suggests that the range of relatively simple models adopted by Delaygue and Bard (2010) might overestimate the uncertainties than we can expect.

Geomagnetic field behaviour: Our approach eliminates to a large extent uncertainties in the geomagnetic field intensity. Nevertheless, even if there is no evidence for significant and strong geomagnetic dipole field intensity changes on time scales shorter than 500 yr such changes cannot be excluded. This contributes to the uncertainties in the inferred solar activity variations on shorter time scales and such changes would then still be visible in Fig. 4. However, a systematic geomagnetic field-related bias of the amplitudes of the variations shown in Fig. 4 is unlikely.

Limited data resolution: There is no high-resolution cosmogenic radionuclide record with high enough resolution to trace the solar 11-yr cycle throughout the Holocene. Figure 3 shows that the 11-yr cycle adds to the variability even during periods of a very quiet Sun. Comparison of Fig. 3 and Fig. 4 indicates that the amplitude discussion should be narrowed down by about 10% to accommodate for the fact of the varying solar activity even during periods of a quiet Sun. This does not apply for the high solar activity levels since we did the comparison to an average solar modulation of the last 60 yr.

6 Conclusions

With an analysis of the range of variability of cosmogenic radionuclide record we obtain lower limits for the solar activity levels during the Holocene. Overall, there are several uncertainties involved in this discussion. However, the majority of the uncertainties would lead to even larger inferred solar amplitudes (new LIS, data-related smoothing, absence of the shorter-term (< 50 yr) solar variability). Some uncertainties could lead to smaller amplitudes (noise in $^{10}\text{Be}$, carbon cycle bias in $^{14}\text{C}$ calculation) and some uncertainties cannot be quantified (short-term geomagnetic field changes). Even if we base our conclusions on a very conservative approach with probably overestimated effects of solar modulation and using smoothed data (e.g. $^{14}\text{C}$) we obtain evidence that present solar activity levels were not unique and that these occurred on a regular basis. Especially for periods of highly variable $^{10}\text{Be}$ and $^{14}\text{C}$ production rates (e.g. around 5000 yr BP, 2500 yr BP, 500 yr BP) we can conclude that the solar modulation occasionally equalled or exceeded recent levels. It is very likely that the GISP2 and $^{14}\text{C}$ data underestimate the production rate variations due to data-related smoothing which suggests that there are more periods that can be constrained in a similar way (e.g. around 10 000 yr BP). Future progress in understanding the geochemical behaviour of $^{10}\text{Be}$ and $^{14}\text{C}$, improved $^{10}\text{Be}/^{14}\text{C}$ production rate calculations and LIS spectra can lead to even stronger constraints about past solar activity levels with our method. Since we estimate the lower limits only we cannot rule out that sustained levels of higher solar activity occurred in the past.

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